Solutions to Sample Final Exam

Problem 1

(((a b c) a b c))

(((a) a) a)

((a a) b)
**Problem 2**

```
(define (map-two-streams f s1 s2)
  (cons-stream (f (stream-car s1))
               (map-two-streams f
                                (stream-cdr s1)
                                (stream-cdr s2))))

(define (min-two-streams s1 s2)
  (map-two-streams min s1 s2))
```

There is one multiplication done to compute each element of the stream, so the nth element will need n multiplications. However, if the answer was already computed, no multiplications would be necessary. Or if the (n-1)th element had been computed, just one more multiplication is necessary.

This is a bit of a trick question. The nth element still needs n multiplications to be computed. However, if we ask for the (n+1)th element after computing n, we’ll need to redo all of the prior n multiplications since we’re not using memoization.

**Problem 3**

```
(define (make-opl-lecturer name birthplace threshold)
  (let ((person (make-person name birthplace threshold)))
    (lambda (message)
      (cond ((eq? message 'bring-cookies-to-exam)
                (lambda (self)
                  (let ((location (ask self 'place)))
                    (ask self 'move-to cookie-store)
                    (ask self 'take cookies)
                    (ask self 'move-to location)))))
     ((eq? message 'say)
      (lambda (self stuff)
        (ask person 'say stuff)
        (ask person 'say '(Scheme is fun!))))
     (else (get-method person message))))
```
Problem 4

Insert before application? in mc-eval:

\[
\begin{align*}
&\text{(infix? exp)} \\
&\quad \text{(mc-apply (mc-eval (infix-operation exp) env)} \\
&\quad \text{(list-of-values (infix-operands exp) env)))}
\end{align*}
\]

Rest of necessary code:

(define (infix? exp)
  (or (eq? (cadr exp) 'uml:+)
      (eq? (cadr exp) 'uml:-)
      (eq? (cadr exp) 'uml:*)
      (eq? (cadr exp) 'uml:/)))

(define (infix-operator exp) (cadr exp))

(define (infix-operands exp)
  (cons (car exp) (cddr exp)))

Problem 5

(define (make-frame variables values)
  (if (null? variables)
      nil
      (cons (cons (car variables) (car values))
            (make-frame (cdr variables) (cdr values)))))

Here’s the complete lookup-variable-value function. The underlined portions show what was changed from the original.

(define (lookup-variable-value var env)
  (define (env-loop env)
    (define (scan frame)
      (cond ((null? frame)
          (env-loop (enclosing-environment env)))
            ((eq? var (caar frame)) (cdar frame))
            (else (scan (cdr frame))))
      (if (eq? env the-empty-environment)
          (error “Unbound variable” var)
          (scan (first-frame env))))
  (env-loop env))

The following procedures would need to be changed:

set-variable-value!
define-variable!
add-binding-to-frame!
frame-variables
frame-values
Problem 6

Mark and sweep:

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Root: P2
Free: P9

Stop and copy:

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Root: P10
Free: P12

Stop and copy is better when there is more garbage than good cells. Only the good cells are copied. With mark and sweep, all cells must be touched, regardless of whether they are good or garbage.

Mark and sweep uses (almost) all of the memory, while stop and copy can only use half of the memory for its active space.